



Neuromorphic computing with thermal interactions









Neuromorphic computing

- Human Brain:
- ~ 10^{11} neurons
- ~ 10^{15} synapses
- Power consumption:
 - ~ 20 W



- GPT-3:
- 1.75×10^{11} parameters
- $\sim 10^4~\text{J}$ per query
- Training costs
 - $\sim 10^{13} \text{ J}$

Patterson, David, et al. "Carbon emissions and large neural network training." *arXiv preprint arXiv:2104.10350* (2021).

Marković, D., Mizrahi, A., Querlioz, D., & Grollier, J. (2020). Physics for neuromorphic computing. *Nature Reviews Physics*, *2*(9), 499-510.

Neuromorphic computing

- A query from ChatGPT ↔
 10 minutes of brain activity
- Human brain is $\sim 10^4$ times larger than GPT-3
- We need energy efficient hardware!



Neuromorphic computing



Abdallah, Abderazek Ben, and Khanh N. Dang. *Neuromorphic computing principles and organization*. Berlin: Springer, 2022.



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Vanadium dioxide

Insulator-to-metal transition: $T_c \approx 340K$



Budai, J. D., Hong, J., Manley, M. E., Specht, E. D., Li, C. W., Tischler, J. Z., ... & Delaire, O. (2014). Metallization of vanadium dioxide driven by large phonon entropy. Nature, 515(7528), 535-539.

Thermal Neuristor



Substrate: Al₂O₃







Thermal interactions

- Electrically isolated
- Heat propagation through Al₂O₃ substrate





Qiu, E., Salev, P., Torres, F., Navarro, H., Dynes, R. C., & Schuller, I. K. (2023). Stochastic transition in synchronized spiking nanooscillators. *Proceedings of the National Academy of Sciences*, *120*(38), e2303765120.

Thermal interactions





Qiu, E., Zhang, Y. H., Di Ventra, M., & Schuller, I. K. (2023). Reconfigurable cascaded thermal neuristors for neuromorphic computing. *Advanced Materials*, 2306818.

Excitatory interaction



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Inhibitory interaction



Thermal neuristor array



2D array



64x64 neurons



Zhang, Y. H., Sipling, C., Qiu, E., Schuller, I. K. and Di Ventra, M. (2023). Collective dynamics and long-range order in thermal neuristor networks. arXiv preprint arXiv:2312.12899



Y.-H. Zhang, C. Sipling, E. Qiu, I. K. Schuller, M. Di Ventra, (2023). Collective dynamics and long-range order in thermal neuristor networks. arXiv preprint arXiv:2312.12899

Long-range order?

$$C\frac{dV}{dt} = \frac{V_{in}}{R_{load}} - V\left(\frac{1}{R_{VO_2}} + \frac{1}{R_{load}}\right)$$
$$C_{th}\frac{dT}{dt} = \frac{V^2}{R_{VO_2}} - S_{env}(T - T_0) + S_{couple}\nabla^2 T + \eta(t)$$







Long-range order?

$$C \frac{dV}{dt} = \frac{V_{in}}{R_{load}} - V \left(\frac{1}{R_{VO_2}} + \frac{1}{R_{load}} \right)$$
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Self-organized criticality

Image credit:

Thermal neuristors



Sandpile model: Self-organized criticality



/SelfOrganizedCriticality/ImplementingTheSandPile.html

slope increases https://runestone.academy/ns/books/published/complex

Addition of

sand grains: — Critical slope

Bak, Per, Chao Tang, and Kurt Wiesenfeld. "Self-organized criticality: An explanation of the 1/f noise." Physical review letters 59.4 (1987): 381. Hesse, Janina, and Thilo Gross. "Self-organized criticality as a fundamental property of neural systems." Frontiers in systems neuroscience 8 (2014): 166.

Avalanche

occurrence:

slope decreases

Long-range order?

Fast spiking dynamics

$$C \frac{dV_{1}}{dt} = \frac{V_{in}}{R_{load}} - V_{1} \left(\frac{1}{R_{VO_{2}}} + \frac{1}{R_{load}} \right)$$
$$C_{th} \frac{dT}{dt} = \frac{V_{1}^{2}}{R_{VO_{2}}} - S_{env} (T - T_{0}) + S_{couple} \nabla^{2} T + \eta (t)$$

Slow memory dynamics



Long-range order?

Fast spiking dynamics

$$C \frac{dV_1}{dt} = \frac{V_{in}}{R_{load}} - V_1 \left(\frac{1}{R_{VO_2}} + \frac{1}{R_{load}} \right)$$

Time
scale $C_{th} \frac{dT}{dt} = \frac{V_1^2}{R_{VO_2}} - S_{env}(T - T_0) + S_{couple} \nabla^2 T + \eta(t)$

Slow memory dynamics



Avalanche size distribution

$$V = 9.96$$
V, $C_{th} = 1$





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Application: MNIST 0ā Input Dynamics. 2 3 4-**Prediction:** 5-0.96 3 10⁰ 6-Accuracy 0.95 Accuracy Train loss Loss 7 -Test loss Test accuracy 8- 10^{-1} 9-**Fully-connected** 0.93 20 5 10 15 0 output layer Epochs

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Reservoir Computing





- Spiking oscillators utilizing insulator-to-metal transition in VO₂
- Interactions mirroring biological neurons
- Phase of long-range order
- Application: reservoir computing



UC San Diego



Thank you!

E.Qiu, P. Salev, F. Torres, H. Navarro, R. C. Dynes, & I. K. Schuller, (2023). Stochastic transition in synchronized spiking nanooscillators. *Proceedings of the National Academy of Sciences*, *120*(38), e2303765120.

E. Qiu, Y.-H. Zhang, M. Di Ventra, I. K. Schuller, Reconfigurable cascaded thermal neuristors for neuromorphic computing. *Advanced Materials*, 2306818.

Y.-H. Zhang, C. Sipling, E. Qiu, I. K. Schuller, M. Di Ventra, Collective dynamics and long-range order in thermal neuristor networks. arXiv preprint arXiv:2312.12899